Fertility and Childlessness in the US

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Various family types

New types of families.

Q: Childlessness is no longer necessarily a fate, it can also be a choice. By whom?
Childlessness

- voluntary: “child-free” (our estimation for US: 8.1%)
- involuntary
  - “natural sterility” (our estimation for US: 2.3%)
  - “social sterility” (our estimation for US: 2.5%)

Understanding the incentives can:

- predict population trends
- enhance welfare (fighting poverty driven childlessness)
Childlessness, more than a special case of fertility (≠0)

Completed Fertility of Mothers vs. Childlessness

By Cohort in the USA (left panel), By Education levels in Brazil, Mexico and the USA (right panel)
What is the share of childlessness that is voluntary?

What is the share of childlessness that is poverty driven?

How do economic changes affect the different family types? In particular, how can we reduce the involuntary part of childlessness?

→ one needs a theory to measure the types of childlessness
A theory to explain jointly marriage and parenthood decisions

Identification of the parameters using moments from Census

Show that co-existence of involuntary and voluntary causes of childlessness is key to explain facts (US, 1990)

Predictions: How better education did affect both types of childlessness and fertility over time.

Policy experiment: How inequality does affect both types of childlessness.
Main features of the model

1. agents are matched randomly, once in life
2. they decide to marry or not
3. they discover their natural fertility status
4. Cooperative decision on consumption and fertility

Women can have children, married or not ≠ Men should marry to have children

Exogenous potential income (education): $w^i$

+ heterogeneity in non labor income $a^i \perp w^i$
Preferences

**Individuals:**

\[ u(c^i, n) = \ln c^i + \ln (n + \nu) \]

No gender differences in preferences
\( \nu > 0: \) Services from children are superior good

**Couples:**

\[ \theta u(c^f, n) + (1 - \theta) u(c^m, n) \]

with

\[ \theta \equiv \frac{1}{2} \theta + (1 - \theta) \frac{w^f}{w^f + w^m}, \quad \theta \in (0, 1) \]

\( \Rightarrow \) although \( \exists \) marriage surplus, one spouse may refuse marriage
Sterility

Natural: $\chi$ and $\zeta$: % of female and male who are naturally sterile

Social: Minimal consumption to be able to procreate: $c^{\text{min}}$

$$n > 0 \Rightarrow c^f \geq c^{\text{min}}$$


1. Malnutrition
2. Poor use more drugs
3. Poor have less access to medical services: if they want to abort, they may be sterile after a medical mistake + no access to IVF
4. Poor live in more polluted areas: ↓ fecundity
Time constraints

Endowment per person: 1 if married; \(1 - \delta^f\), \(1 - \delta^m\) if not

First child costs \(\phi(1 + \eta)\) units of time
Additional children cost \(\phi\) units of time

Singles: mothers support the time cost of children alone

Married’s: \(\alpha \in (\frac{1}{2}, 1)\) mother’s share of child support (exogenous)

Upper bound on number of children one can have:

\[
0 \leq n \leq \frac{1 - \delta^f - \phi \eta}{\phi} \equiv \bar{n}_M(\text{singles})
\]

\[
0 \leq n \leq \frac{1 - \alpha \phi \eta}{\alpha \phi} \equiv n_M(\text{couples})
\]
Budget constraints

**Single men:**

\[
b^m(c^m) = c^m - (1 - \delta^m)w^m - a^m + \mu \leq 0.
\]

\(\mu\): cost of running a household

**Single women:**

\[
b^f(c^f, n) = c^f + \phi (1 + \eta(n)) w^f n - (1 - \delta^f)w^f - a^f + \mu \leq 0
\]

**Couples:**

\[
b(c^f, c^m, n) = c^f + c^m + \phi (1 + \eta(n)) \left(\alpha w^f + (1 - \alpha)w^m\right) n
\]
\[
- w^m - w^f - a^m - a^f + \mu \leq 0.
\]
Value functions

\[ V^{s,m} = \max\{u(c^m, 0); b^m(c^m) \leq 0\} \quad \text{[single male]} \]

\[ V^{s,f} = \max\{u(c^f, n); b^f(c^f, n) \leq 0, \quad 0 \leq n \leq \bar{n}_M, c^f < c^\text{min} \Rightarrow n = 0.\} \quad \text{[single female]} \]

\[ \tilde{V}^{s,f} = \max\{u(c^f, 0); b^f(c^f, 0) \leq 0\} \quad \text{[single sterile female]} \]

\[ V^{\omega,i} = u(c^i, n) \text{ where} \]
\[ \{c^f, c^m, n\} = \arg\max\{U(c^f, c^m, n); b(c^f, c^m, n) \leq 0, \quad 0 \leq n \leq n_M, c^f < c^\text{min} \Rightarrow n = 0.\} \quad \text{[married]} \]

\[ \tilde{V}^{\omega,i} = u(c^i, 0) \text{ where} \]
\[ \{c^f, c^m\} = \arg\max\{U(c^f, c^m, 0); b(c^f, c^m, 0) \leq 0\} \quad \text{[sterile married]} \]
Marriage if

\[(\chi + (1 - \chi)\zeta)\tilde{V}^{\omega,f} + (1 - \chi)(1 - \zeta)V^{\omega,f} \geq \chi\tilde{V}^{s,f} + (1 - \chi)V^{s,f}\]

\[(\chi + (1 - \chi)\zeta)\tilde{V}^{\omega,m} + (1 - \chi)(1 - \zeta)V^{\omega,m} \geq V^{s,m}\]
Regimes given Marriage Decision

Depending on which constraint binds, people can be in six different situations:

[N] Natural sterility,
[S] social sterility when $n > 0 \Rightarrow c^f \geq c^{\text{min}}$ binds and $n = 0$,
[M] maximum fertility when the time constraint, $n \leq \bar{n}_M$ or $n \leq n_M$, binds,
[C] constrained fertility when $n > 0 \Rightarrow c^f \geq c^{\text{min}}$ binds and $n > 0$,
[V] voluntary childlessness when the constraint $n \geq 0$ binds, and, finally,
[U] unconstrained fertility.

Conditionally on being married or not, $\exists$ thresholds for wages and non-labor income separating different regimes.
Fertility conditionally on being married when $a^f \in [A_0, A_1]$
Fertility conditionally on being married when $a^f \in [A_1, A_2]$
Data: US Census, 45-70 year old married and never married women in 1990. **Completed fertility**

Drop Separated, Widowed and Divorced (≈ 30%), concentrate on Married and Single

Potential income - 12 education categories - 1127080 obs

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<th>Category</th>
<th>N. obs.</th>
<th>Nb</th>
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**Fact 1: fertility** Fertility of mothers decreases with education, for both married and single women.
Fact 2: **childlessness** Childlessness exhibits an U-Shaped relationship with education for both singles and married.
**Fact 3: marriage** There is a hump-shaped relationship between marriage rates and education levels for women. Marriage rates (weakly) increase with education for men.
Identification of the Parameters

Fix some parameters a priori

For the others: We minimize

\[ [d - s(p)] [W] [d - s(p)]' \]

- \(d\): vector of 72 moments from Census
- \(p\): vector of 11 parameters
- \(s(p)\): vector of simulated moments
- \(W\): weighting matrix.
Some parameters are fixed a priori

**WAGES**

Potential labor income depending on education

\[ w_e = \gamma \exp\{\rho e\}, \]

\[ \gamma = 0.869, \ \rho = 0.092 \text{ (estimated on census data)} \]

**STERILITY**

\[ \chi + (1 - \chi)\zeta = 0.024 \text{ (childlessness rate of Hutterites)} \]

\[ \chi = \zeta = 0.0121 \]
How the simulated moments are computed

For each woman we draw

- a non labor income from a log-normal distribution (mean and variance are parameters to be identified)
- a potential husband, with random education level and non-labor income

We compute whether each potential couple will marry, and what will be the optimal fertility of the woman

Simulated moments obtained by aggregating all individual choices
### Identified parameters

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<th>Description</th>
<th>Value</th>
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<td>Variance of the log-normal distribution</td>
<td>$\sigma_a$</td>
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<td>Average ratio of non-labor income to labor income</td>
<td>$\bar{m}_a$</td>
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<td>Preference parameter</td>
<td>$\nu$</td>
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<td>Minimum consumption level to be able to procreate</td>
<td>$c_{\text{min}}$</td>
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<td>Good cost to be supported by a household</td>
<td>$\mu$</td>
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<td>Bargaining parameter</td>
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<td>Fraction of childrearing to be supported by women</td>
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<td>Time cost of having children</td>
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<td>Fixed cost of children</td>
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<td>Time cost of being single (men)</td>
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<tr>
<td>Time cost of being single (women)</td>
<td>$\delta^f$</td>
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Childlessness and Completed Fertility of Mothers, Married Women
Childlessness and Completed Fertility of Mothers, Single Women
Marriage Rates of Women and Men
Overidentification check

Completed Fertility of Married Fathers (left), Childlessness rates of Married Men (right), by Years of Schooling. Data (black), Simulation (grey), Education Categories (labels)
### % of women in each regime by education category

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Causes of childlessness

- Involuntary childlessness (biological)
- Voluntary childlessness
- Involuntary childlessness (social)
Historical experiment

Fertility and childlessness rate of married women

General trend in captured.
Non linear interaction between education and TFP.
Two events are not captured: baby boom, super high childlessness in 1900
Historical experiment

Simulated Childlessness by Cohort, Married (left) and Singles (right)

Social sterility has disappeared for married, but not for singles
Childlessness Rate for Different Levels of Inequality (Mincer Coefficient)

Grey Line is the Benchmark $\rho = 0.092$ and Dotted Line is the Historical Maximal $\rho = 0.126$. 
Childlessness Rate & gender wage gap $\gamma$

\[ \gamma = 0.755 \text{ (dashed), } \gamma = 0.869 \text{ (solid), and } \gamma = 1 \text{ (dotted)} \]

Usual opportunity cost effect on fertility

Drop in Involuntary Childlessness and rise in Voluntary Childlessness
Conclusion

Distinguish decision to have children from choice of their number

New “regimes” of fertility, relevant in the data:
- 4.8% of American women are involuntarily childless in 1990
- 8.1% are voluntarily childless

Co-existence of regimes explains U-shaped relationship between childlessness and education (for both married and single women)

Marriage interacts with childlessness:
- for low skilled woman ⇒ marriage gives more resources to be able to have children ⇒ reduces involuntary childlessness.
- for high skilled women, marriage reduces opportunity cost of having children ⇒ reduces voluntary childlessness.

Reducing inequality helps fighting social sterility